

7664

DESCRIPTION and USE
of the
PATENT
Military and Naval
Telescope,
for Measuring
Distances and the Extension of Objects
at
SIGHT;
By means of a new Micrometrical adjustment.
DEDICATED BY PERMISSION
To His Royal Highness
Duke of York



THE Poppleton Press

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DEDICATION.

TO HIS ROYAL HIGHNESS

THE DUKE OF YORK,

BISHOP OF OSNABURGH,

FIELD MARSHAL, COMMANDER IN CHIEF

HIS MAJESTY'S FORCES, &c. &c.

Sir,

WHEN I HAD THE HONOUR OF BEING INTRODUCED
TO YOUR ROYAL HIGHNESS, TO EXPLAIN THE PRIN-
CIPLES OF A MILITARY TELESCOPE, WHICH I HAD
ORIGINALLY CONSTRUCTED FOR THE PRIVATE USE

DEDICATION.

OF THE RIGHT HONOURABLE THOMAS PELHAM, FOR
 ASCERTAINING DISTANCES, AND THE EXTENSION OF
 OBJECTS AT SIGHT, BY MEANS OF AN ENTIRELY NEW
 MICROMETRICAL ADJUSTMENT; I WAS HIGHLY
 FLATTERED BY YOUR ROYAL HIGHNESS'S PROFES-
 SIONAL OBSERVATIONS ON IT, AND GREATLY GRATI-
 FIED THAT IT MET THE APPROBATION OF A PER-
 SONAGE SO EMINENTLY QUALIFIED TO DECIDE ON
 ITS GENERAL AS WELL AS ITS PARTICULAR MERITS.

THE FIELD OF THE MICROMETER HAVING BEEN
 SINCE VERY CONSIDERABLY ENLARGED, IS AN IM-
 PROVEMENT WHICH, AS IT ENCREASES THE UTILITY
 OF THE TELESCOPE FOR THE ARMY, RENDERS IT
 ALSO OF EQUAL IMPORTANCE TO THE NAVY, AND
 FOR ALL GENERAL PURPOSES, WHERE ASCERTAINING
 THE DISTANCE OR THE EXTENSION OF OBJECTS IS
 REQUIRED.

PATRONIZED BY YOUR ROYAL HIGHNESS, I HAVE
 THE HONOUR OF DEDICATING TO YOU THE FOL-
 LOWING PAGES, EXPLANATORY OF THE PRINCIPLES,

AND

DEDICATION.

iii

AND ILLUSTRATIVE OF THE VARIOUS USES AND ADVANTAGES OF THE MILITARY AND NAVAL TELESCOPE.

I HAVE THE HONOUR TO BE,

SIR,

YOUR ROYAL HIGHNESS'S

MUCH OBLIGED,

MOST OBEDIENT, AND MOST DEVOTED

HUMBLE SERVANT,

CATER RAND.

LEWES, FEB. 1, 1799.

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DECLARATION

AND AFFIRMATION OF THE VARIOUS OFFICERS AND

MEMBERS OF THE SENATE AND HOUSE OF REPRESENTATIVES

IN THE YEAR 1862

AND IN THE YEAR 1863

AND IN THE YEAR 1864

AND IN THE YEAR 1865

AND IN THE YEAR 1866

AND IN THE YEAR 1867

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ERRATUM.				
In the Note, page 8, for "Cap-pieces" read "Tube."				
DESCRIP-				

Fig. 3.

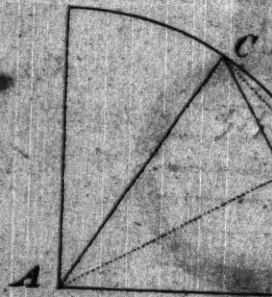


Fig. 4.

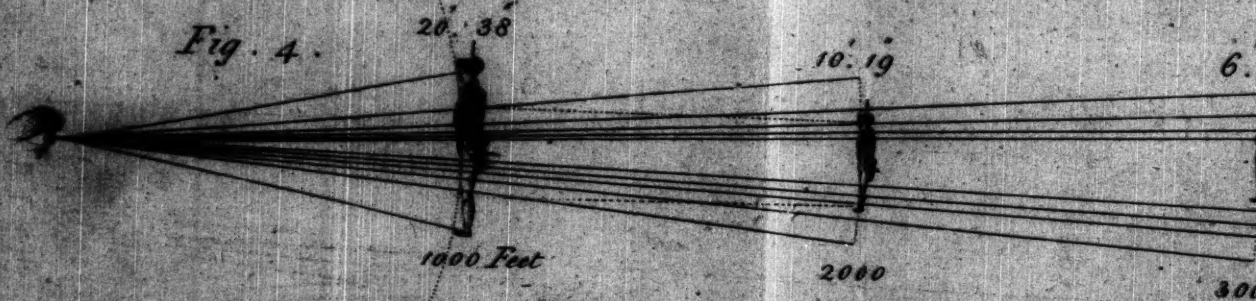


Fig. 5.

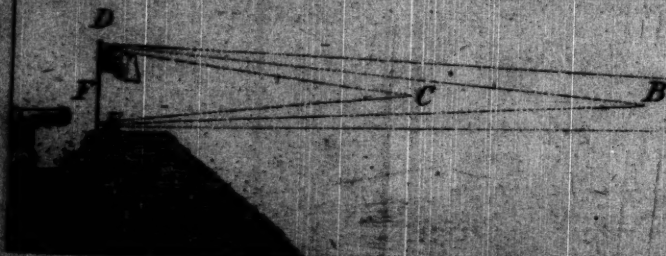
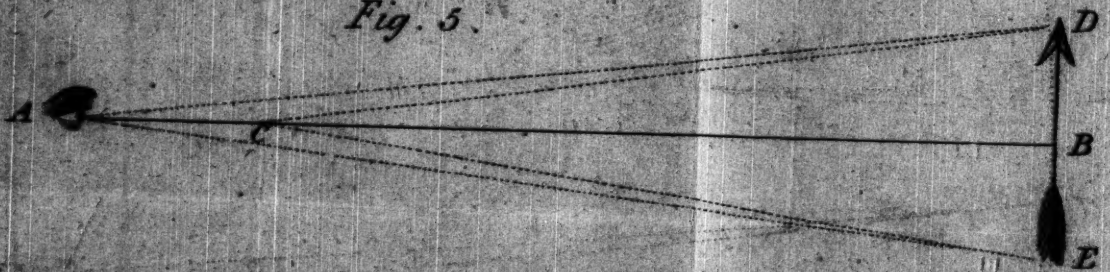


Fig. 7.

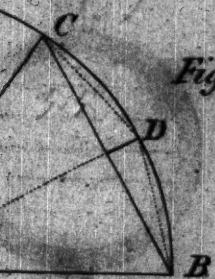


Fig. 2.

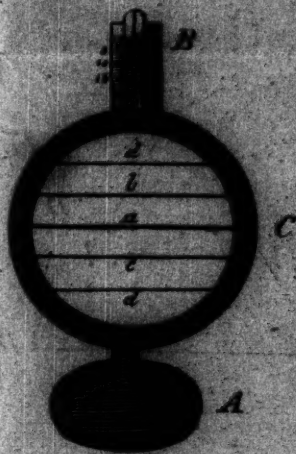


Fig. 1.

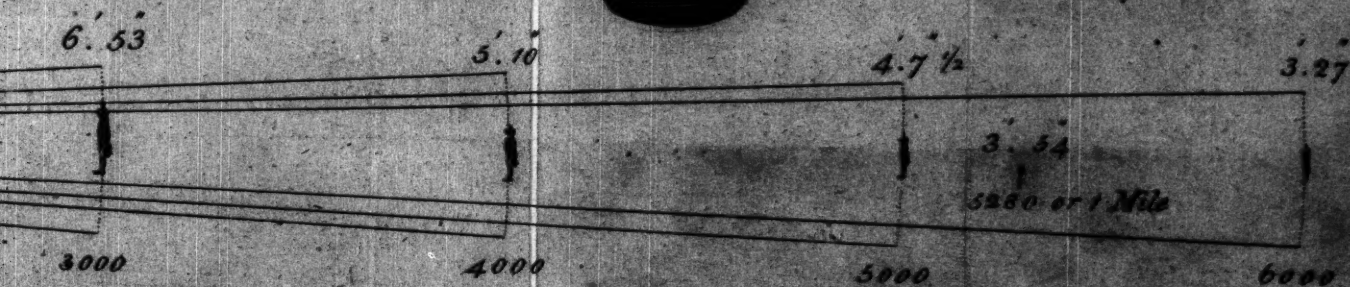
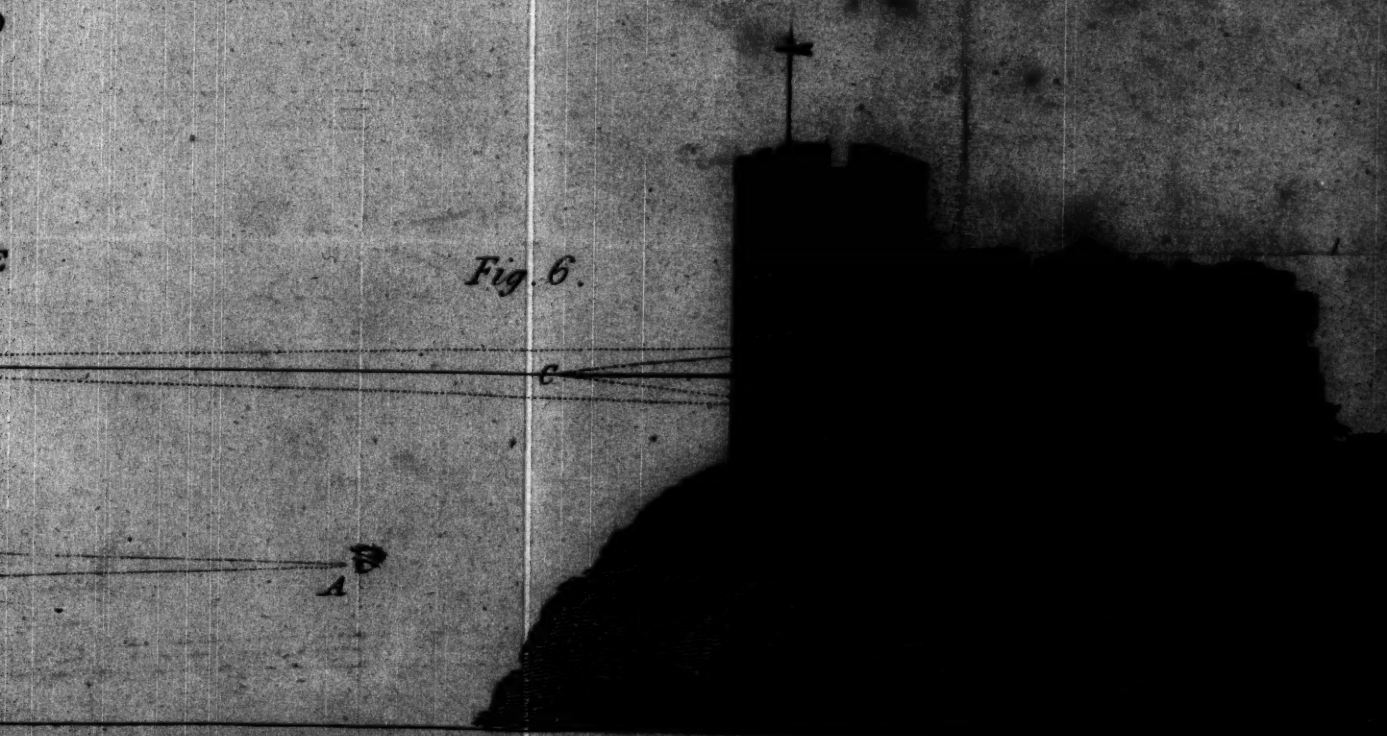


Fig. 6.





DESCRIPTION, &c.

THERE is nothing new in the application of a Micrometer to a Telescope, for measuring small angles or distances. The Patent one, however, about to be described, differs very materially from any thing of the kind ever offered to the public; and will be found far superior to any other in its application to all the various purposes to which it is more peculiarly adapted.

It has long been a *desideratum* to measure the distance of objects at *one* station, instead of *two*, as hitherto practised, from the ends of a base-line; and some ingenious contrivances have been suggested for that purpose; but no

instrument has yet been made at all calculated to obtain that end.

DESCRIPTION.

The fixed Mother-of-Pearl Micrometer of Mr. CAVALLO's, situated in the Focus of the Eye-glass, could the objects be defined to that degree of precision necessary to measure the angle subtended with accuracy and truth, would, from its simplicity and cheapness, be of great public benefit. The instrument described in Vol. I. of the Repertory of Arts, page 163, invented by Mr. JAMES PEACOCK, of Finsbury-square, Architect, for measuring distances from one station only, is certainly ingenious; and the "idea of a Dendrometer, or instrument, for measuring distances by one observation, by W. BIRN, Esq. of Pendeford, near Wolverhampton," is still more ingenious; and had he followed up his idea by the construction of an instrument something similar to the one described in

the

the same Work, Vol. II. page 238, it would have superseded, in a great degree, the necessity of the Patent one. The telescopic part of the Patent Instrument for measuring distances, &c. as one station, is of the best possible construction; and the micrometrical peculiarly adapted to answer all the purposes for which it is designed, as will be amply set forth in the following pages, and illustrated by a great variety of examples, in real practice. To give an historical account of the Micrometer, its invention, use, various construction, and application, as well to the Microscope as the Telescope, would too far exceed the limits of a mere descriptive pamphlet, explanatory of its principles adapted to the Telescope only. To persons desirous of further information, the Encyclopædia Britannica; Hutton's Mathematical and Philosophical Dictionary; the Philosophical Transactions, &c. &c. may be consulted.

When the Micrometer is adapted to the Microscope, it is to measure lineal extensions, as the length, &c. of the smallest insects, the diameter of a hair, &c. &c. but when adapted to the Telescope, it is for the more immediate purpose of measuring small angles, and thence the distance of objects, as will be fully explained, to the entire satisfaction of every person who may be in possession of the Patent Telescopic Micrometer.

Although the Patent Telescope may be made of different sizes or lengths, some with slides, others in one length, as those usually made for the Navy, yet the principle of each, and of every shape and size, will be the same; they will all answer the same precise purpose, and measure the several distances or extension of objects, with one and the same degree of accuracy. It may be proper to observe, that the Patent Telescope, besides the advantages arising from its peculiar construction for the
more

more immediate use of the Army and Navy, in measuring distances, &c. at sight, by one or more observations, has all the properties in common with other Telescopes, for viewing objects on the horizon, or for celestial observations of any kind; in measuring the apparent diameters of the sun, moon, and planets; the cusps of the moon in eclipses; the distance of the satellites from their respective planets; the distance between a planet, star, and the moon, approaching to, or receding from, occultations, &c. It may also be used as a Microscope, as will be hereafter described.

The Micrometer adapted to the Patent Telescope has both a *fixed*, as well as a *moveable*, value; and herein its principles differ from any other;—and it has a field sufficiently large to answer every purpose to which it can be applied; or to which it is intended to be applied by the artillerist or nautical observer, in the mensuration of distances, &c. or to the curious in *their* observations;

vations; either in viewing objects, as a common Telescope, before mentioned, or minute objects, as a Microscope.

The principles then of the micrometrical part of the Patent Telescope, and wherein it differs from *all* others, are these: as above observed, it has a *fixed*, as well as a *moveable*, value, to ascertain the angle subtended by any object to be measured by it, as the diameter of the sun, the distance between two stars, the height of a man, the *angle* subtended by any cape or head-land, viewed at sea; a fort, church, or mill; or any remote object, *whereby* the respective distances, &c. may be found from the place or places of observation; and this without any previous knowledge of trigonometry, and the tedious method by logarithmic calculations; but, as it were, by inspection only, by merely entering the table of horizontal distances, at page 24, with the subtending angle of the object, and, corresponding thereto, the respective distance may

may be found without any further trouble or difficulty, than computing the several distances, and bringing them into such measure of yards, feet, inches, or other measure, as may be required, or the extension of the objects happen to be given in.

EXPLANATION OF THE SEVERAL FIGURES IN THE PLATE.

Fig. 1. A. B. C. shews, in plano, the Micrometer of the Telescope; A. the Nut, or Screw-head, that regulates the mechanism of the parts, and gives motion to the several parallel hairs, or wires, *a. b. c.*—*a.* being a double hair, or wire, that, on the motion of the parts behind C. the protuberant part of the Eye-tube of the Telescope, by means of the Nut, or Screw-head, at A. opens parallel to the extent of *b.* and *c.* which, at the same time, and regulated

lated by the same motion of the Nut, move parallel and to the dotted lines, *d. d.* whose respective distances, or parallel openings, forming an angle, the eye being the focus, are accurately measured by the Scale at B. to which a Vernier, or Nonius, is adapted, that measures the subtending angle of any object, within its field, to seconds of a degree.

The relative situation of the parallel hairs, or wires, *b. c.* are to give the Instrument a larger field; and, as their value at rest, or in motion towards the dotted lines, *d. d.* when an angle subtends larger than the field of the double line *a.* is given, the subtending angle of any object, within the *whole* field of the Instrument, may be easily obtained, by only adding the known value of *b. c.* at a fixed value from *a.* to the value of the double lines *a.* opened to their full extent, read off the scale B.*

The

* The fixed value will be engraved in the Cap-pieces of every Telescope.

The Micrometer, with all its adjustments, is placed in its proper situation in the Eye-piece of the Telescope; and for reading off the fine divisions of the scale B. with its Vernier or Nonius, a small Lens is placed before it; but which could not, without confusion, be shewn in the figure.

The scale of the Micrometer is divided into hundredths of an inch; and, when the Vernier points to the first division, the hairs or wires will all stand exactly parallel to each other, as in the figure; the double hairs or wires at *a* appearing as one.

Suppose two lines to be drawn from the opposite edges of the sun's disc, from those of the moon, or any other object, to the eye of the observer; viewing either of the above objects through the Telescope, the angle formed by such lines, converging to the eye, is measured by the Scale of the Patent Micrometrical Telescope to minutes and seconds of a degree.

C

To

To measure the angle subtended by the sun, or its apparent diameter, (*the apparent diameter of the sun varies in the course of the year about one minute of a degree, appearing under the largest angle in the month of January, and the smallest in the month of July,*) apply the Telescope, with the dark glass-slide before the eye, to the sun, and by means of the Nut or Screw-head A. open the moveable parallel hairs or wires *a*. till the upper and lower edges of the sun's disc are neatly defined between the center hairs or wires of the Instrument; then will the Index on the Scale, by means of the Vernier or Nonius, point out the minutes and seconds of a degree that the sun's disc subtends at that time.

For example:—On the first of July, wanting to know the apparent diameter of the sun, by applying the Telescope, with the dark glass on, as before directed, to the sun, the parallel hairs or wires, to subtend the angle of the diameter or whole disc, have moved the

the Index on the Scale over fifteen divisions; and the Vernier or Nonius stands at about 78 hundredths, which, as will be presently shewn, equals $31' 34''$ nearly. The Nautical Almanack, for the same day, gives the sun's semi-diameter $15' 46''.9$, or $31' 33''.8$, for its whole diameter; varying but two tenths of a second from the instrumental measure by the Patent Telescope.

Again:—If, on the first of January, the Telescope be applied to the sun, as before directed, it will be found that the angle subtended by the sun's disc, or whole diameter, will pass sixteen divisions on the scale, and that the Vernier or Nonius will stand at about 33 hundredths, which will be found equal to $32' 39''$ nearly, the apparent diameter or angle the sun subtends on *that* day: The Nautical Almanack, for same day, gives $16' 19''.4$ for its semi-diameter, or $32' 38''.8$ for its whole diameter, varying, as before, about two tenths

of a second, or $12''$ of a degree of a great circle.

To explain in what manner fifteen divisions on the Scale, and the Vernier or Nonius standing at about 78 hundredths, is equal to $31' 34''$, and in this way to find the value of any subtending angle, within the field of the Instrument, which, for all the purposes intended, whether for the use of the army, the navy, or for common telescopical observations, is sufficiently extensive, this is *The Rule*:—Let the Micrometer divisions passed over by the Index, and the parts pointed out by the Vernier or Nonius, be always DOUBLED; the reason of this is, the parallel hairs or wires move through *twice* the space that the Index on the Scale does: hence the necessity of *doubling* the divisions on the Scale, to measure the apparent angle subtended by any object, as the diameter of the sun or moon, the distance between the moon and a planet, or star, preceding an occultation;

cultation; the subtending angle of a distant cape or head-land; a ship at sea; a fort or gar-
rison; mill, church, or other object; the ca-
valry or infantry of a stationary, approaching,
or receding army, &c. &c. The divisions on
the Scale, *doubled*, as above directed, measure
the subtending angle in parts of a great circle.
For instance,—the Index, as before-mentioned,
when the Telescope was applied to find the
apparent diameter of the sun on the 1st of July,
stood at *fifteen* divisions on the Scale, and the
Vernier or Nonius at about 78 hundredths, which
being *doubled* gives 30' 156 of the hundredths,
or 31' 34"; for every Vernier or Nonius tenth
equals 6" of a degree of a great circle; con-
sequently 156 hundredths, the *double* of 78
hundredths, pointed out by the Vernier or
Nonius, is equal to 1' 34"; which, added to
the *doubled* divisions, *fifteen*, pointed out by the
Index, makes the apparent diameter of the sun
for that day, as before shewn, 31' 34" nearly;
the angle subtended by the sun's disc.

Again,

Again :—Viewing a castle at a distance, to measure its subtending angle—it appears the index has passed the fourth division on the Scale, and that the Vernier or Nonius stands at 20 hundredths; *doubling* 20 hundredths makes 40, which, at 6" for every 10 hundredths, equals 24"; this added to the *double* of the whole divisions 4, makes the angle subtended by the castle 8' 24" of a degree of a great circle.

One example more will be sufficient to explain the use of the Scale, the Vernier or Nonius divisions, and the manner of reading off the angle.—Applying the Telescope to a centinel on a distant garrison, it appears that he subtends an angle of 4' 12": for the Index stands a little below the *second* division on the Scale, which *doubled* gives 4', and the Vernier or Nonius at the same time cuts *one* tenth, or ten hundredths, equal to 6", which also *doubled* give 12", and added to the two divisions *doubled*, makes 4' 12", the apparent angle subtended by the centinel at the garrison. To find the angle

angle subtended in all cases, *double* the divisions on the Scale, pointed out by the *Index*, as well as the *Vernier* or *Nonius*; the whole divisions will be equal to *degrees*, and *minutes* of a great circle, if above 60; and every tenth of the *Vernier* or *Nonius* will be equal to $6''$ of a degree of a great circle, as above observed.

NOTE. As the Patent Telescopic Micrometer may fall into the hands of persons unaccustomed to, or totally unacquainted with, the use of the *Vernier* or *Nonius*, it may be proper to give the following concise explanation of it.

The *Vernier's*, or *Nonius* Scale, is a small graduated scale, which ~~is placed on~~ the side of the Micrometer Scale B. Fig. 1. and the value of its divisions are read off thus: If the *Index*, as in the last example, stands between the second and the third division on the Micrometer, or left-hand Scale, the division of the *Vernier* or *Nonius* Scale, that is seen to coincide with a division of the Micrometer, or left-hand Scale, points out its *value* in tenths or centesms; every tenth of which equals $6''$ of a degree: so that the *two* whole divisions on the larger Scale, and the *one* tenth on the *Vernier* or *Nonius*, equal when *doubled*, four minutes and two tenths, or twenty centesms, or $4' 12''$, and so of any other value, always allowing $6''$ for every tenth on the *Vernier* or *Nonius* Scale. A little practice will soon familiarise the reading off the divisions on both Scales to a very great nicety.

It

It is hoped the *above* explanation of the *value* of the Micrometer's Scale is sufficiently elucidated to enable any person to find the angle subtended by an object, with which he is to enter the following Table of Horizontal Distances, to find out the true distance of the object, and, from the place of observation, as will be shewn by a sufficient variety of examples, to prove the great usefulness, and superior advantage, of the Patent Instrument above any thing of the kind for Military and Naval purposes, where the ascertaining distances, and the size or extension of objects is promptly required.

Having sufficiently explained the mechanical effects of the Micrometer, and shewn how to find the *value* of an angle for ascertaining the distances and extension of objects, by means of the Table of Horizontal Distances; for the satisfaction of those who may wish to know on what principles the Table is made, Fig. 2. is introduced.

It

It is not intended to enter into any abstruse mathematical calculation, serving rather to *puzzle* and *confound*, than to convince those for whose use this short descriptive pamphlet is written. Every thing, therefore, will be explained in the most simple and familiar manner; so that persons, knowing little more of the science of numbers than that *two* and *two* make *four*, may use the Patent Instrument with as much address as the ablest Mathematician, by following the mere mechanical rules and directions given; nevertheless, to go fully into the explanation and construction of the Table, some calculation is necessary, and may be expected by those somewhat familiar in these things.

Fig. 2: is the quadrant of a circle, the angle C. A. B. is isosceles, subtending the arch line C. D. B. of the quadrant $57^{\circ} 17' 42''$, which measures the length of the arch line, C. D. B. exactly equal to radius A. B. There are several

D

ways

ways of proving this; one or two simple examples will be fully sufficient in the present instance:

The radius of a circle being 1, the semi-circumference is 3.14159, &c. this number, divided by the degrees in a semi-circle, 180, gives, .01745329, for the length of one degree, the radius being unity.

To find the length of the arch line C. D. B. multiply continually the radius, the number of degrees in the given arch, and the above number, .01745329 the product will give the length of the arch line.

Or,

Multiply the chord of half the segment, C. D. or D. B. by 8, and from the product subtract the chord of the whole segment, C. B. the remainder, divided by 3, the quotient will be the length of the arch line C. D. B. nearly.

Let

Let the radius A. B. equal 71; the chord of the *whole* segment C. B. equal 67; the chord of *half* the segment 35:— $71 \times 57^{\circ} 29' 5'' \times .01745329 = 71$, the length of the arch line C. D. B. *i. e.* 71, the radius, multiplied into $57^{\circ} 17' 42''$, or $57^{\circ} 29' 5''$ —(.295 being the decimal of $17' 42''$) and this product into .01745329, the decimal length of one degree; the radius being *unity*, gives 71 as above, the length of the arch line equal to radius; and by this method the arch line is found, let the given radius be what it may:—

Or,

The chord of *half* the segment C. D. or D. B. = 35, multiplied by 8, and the *whole* segment C. B. = 67 subtracted from the product, the remainder, divided by 3, gives also the arch line C. D. B. equal to radius 71 given;—and so of any other proportion.

$$\begin{array}{r} 35 \\ \times 8 \\ \hline 280 \\ 67 \\ \hline 3 \overline{) 213} \end{array}$$

Arch line C. D. B. equal 71 as before.

Hence the Table for computing the Horizontal distances of objects, calculated to seconds of a degree.

Hence also, the reason why the Tabular number, corresponding to the angle subtended by any object, becomes the *multiplier* to find the distance, when the extension is known; or the *divisor* to find the extension, when the distance is known; or to be used, as circumstances occur, when *neither* distance nor extension is known, but *one* or *both* required.

The angle subtended to make the arch line equal to the radius, is, as above, $57^{\circ} 17' 42''$, or $3437' 42''$ —but in the Table, 3438 is made use of, as the nearest *whole* number, the difference being immaterial;—where decimals are used, they are to be understood to be those the nearest to .25 .50 or 75 hundredths.

To find out the nearest numbers corresponding to a measured angle, suppose, for instance,

15'

15' 25"—seek 15' in the *left* hand column of the Table, and under 20", in the Horizontal line, stands 224, and under 30" stands 222, these sums being added together give 446, the *half* of which is 223, the mean between 20' and 30', or the angle of 15' 25": and in this way the intermediate number of seconds may be found, to any proportion required, even to a single second.

Thus having described the mathematical as well as the mechanical principles of the Patent Telescope, at least as far as it is necessary, to its application in practice,—it remains to shew the great variety of purposes to which it may be applied, not only as a military or naval instrument, as heretofore mentioned, but as an equally amusing, and more generally useful Telescope than any other, for all the civil purposes of society.

Those Telescopes constructed for *general* use are of the sliding portable sort, made as plain and

and simple as possible, to avoid expence; they may be made, however, in any way required, either for the *pocket*, or fixed on a *stand*, as occasionally wanted. The common portable sliding fort are, upon the whole, best adapted to military uses; those in one length for naval; and those mounted on a stand for the observatory or summer-house.

In the following Problems and Examples brevity of description, with clearness of information, will be studied; and the several explanatory figures being as simple as lines could form them, no technical phraseology will be used, further than what is absolutely necessary to illustrate and give full value and effect to each; so that every person may fully comprehend their usefulness when practically applied.

To persons, indeed, used to trigonometrical calculations, with the help of logarithmic tables, every thing may appear simple; the

Table

Table of Horizontal Distances will, however, be found useful, and save much labour and trouble to them; but to those unacquainted with the rules of trigonometry and the uses of logarithmic tables, the Table of Horizontal Distances becomes *absolutely* necessary; and, as hath been before observed, may, with a little practice, be used with as much address, and truth, by those unacquainted with the mathematics or its principles, as by the deepest read in that *noble science*.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42																																																										

TABLE
FOR
COMPUTING THE HORIZONTAL DISTANCE, &c.
OF OBJECTS,
FROM THE PLACE OF OBSERVATION.

	0"	10"	20"	30"	40"	50"
0	0	0	0	0	0	0
1	3438	2946	2579	2292	2063	1875
2	1789	1586	1478	1379	1298	1213
3	1146	1085	1031	982	938	897
4	859	815	793	764	737	711
5	685	665	645	626	607	589
6	573	559	543	529	516	503
7	491	479	469	458	448	439
8	430	421	412	404	397	388
9	382	375	368	362	355	349
10	344	338	333	328	322	317
11	312	308	303	299	295	291
12	286	283	279	275	271	268
13	264	261	258	255	252	248
14	245	243	240	237	235	232
15	229	227	224	222	220	217
16	215	213	210	208	206	204
17	202	200	198	196	195	193
18	191	189	188	186	184	183
19	181	179	178	176	175	173
20	172	170	169	167	166	165
21	164	162	160.6	159.5	158.4	157
22	156	155	154	153	152	150
23	149.5	148.5	147.4	146	145	144
24	143	142	141	140.4	139.4	138.5
25	137.5	137	136	135	134	133
26	132	131.4	130.6	130	129	128
27	127	126	125.6	125	124	123.5
28	123	122	121	120.6	120	119
29	118.5	118	117.4	117	116	115
30	114.6	114	113	113	112	111.5

AND NAVAL PATENT TELESCOPICAL MICROMETER. 25

	0"	10"	20"	30"	40"	50"
31	111	110.4	110	109	108.6	108
32	107.4	106.7	106	106	105	105
33	104	103.6	103	102.6	102	101.6
34	101	100.6	100	99.6	99	99
35	98	97.6	97	97	96	96
36	95.5	95	94.5	94	94	93.3
37	93	92.5	92	92	91.3	91
38	90.5	90	90.3	89.3	89	88.5
39	88	87.6	87	87	86.5	86
40	86	85.6	85	85	84.4	84
41	84	83.4	83	83	82.4	82
42	82	81.4	81	81	80.5	80
43	80	79.6	79.3	79	78.7	78.4
44	78	78	77.6	77.3	77	76.7
45	76.4	76	75.7	75.5	75	75
46	75			73.6		
47	73			72.3		
48	71.6			71		
49	70			69.4		
50	69			68		
51	67.4			66.7		
52	66			65.3		
53	65			64		
54	64			63		
55	62.5			62		
56	61.4			61		
57	60.3			59.7		
58	59.3			58.7		
59	58.3			57.8		
60	57.3			56.8		

Applying the Telescope to the object B. C.
 To which suppose the distance from the
 fixed

To prove the truth and accuracy of the power of the Patent Telescopic Micrometer for measuring distances, &c. from one or more observations, a measured distance or base-line of 2000 yards, on a dead level, and an object of known extension, was made use of; and for greater distances, several of the stations of the late Trigonometrical Survey, by Major-General Roy, &c. which had been proved, were used. Several very accurate observations were also made at sea, coasting in the English and Irish Channels.

PROB. I.

To find the *distance* of an object from the place of observation, its *size* being known—

EXAMPLE I.—The object B. C. Fig. 3. being known, to determine its distance from the place of the observer at A.

By applying the Telescope to the object B. C. which suppose to be a six-inch ruler or scale,
fixed

fixed on a post, or stuck against a wall, by means of a wafer, let the Nut of the Micrometer-screw be turned till the object be well defined, *i. e.* till the upper and lower edges of the ruler, or scale exactly coincide with the internal sides of the central parallel hairs or wires; then will the Index point out the angle subtended by the ruler or scale; which, being found equal to 15 divisions, on the Micrometer Scale of the Telescope, this *doubled* gives 30', or half a degree of a great circle. With the subtended angle of the object, 30', enter the Table of Horizontal Distances, where, in the first column of figures, on the left hand, and exactly opposite to 30', stands 114.6 in the next column on the right, the tabular number for 30', which shews how many times the distance of the object is greater than its size; if, therefore, this number 114.6 be multiplied into the size of the object, *viz.* the six-inch ruler or scale, the product will give the distance, in such measure as the size of the object is expressed in. The size or extension of the present

sent object being given in inches, viz. 6. these multiplied into the tabular number, before found, 114.6 gives 687.6 inches, or 57 feet 3 $\frac{1}{2}$ inches, for the distance of the object (*the ruler or scale in this instance*) from the place of observation, or rather from the eye of the observer. The converse of this will give the size or extension of the object; for, if the distance, in the above Example, brought into inches, 687.6, be divided by the tabular number, corresponding to the subtended angle of the object $30' = 114.6$, the quotient will be 6, the known size of the object.

EXAMPLE 2.—Suppose the spire of a church be known to measure 50 feet in height, clear of the battlements; and that, viewed through the Telescope, it be found to subtend an angle of $4\frac{1}{2}$ or 4.5 tenths divisions of the Micrometer Scale, equal to $9'$; take out the tabular number for $9'$, as directed above, which is found to be 382, this number multiplied into the known altitude of the spire, 50 feet, gives

19,100

19,100 feet, or a little more than three miles and a half from the place of the observer.

EXAMPLE 3.—Laying off an enemy's battery, at sea, the height of whose flag-staff had been previously ascertained to be 27 feet required its distance from the ship; the angle subtended by the flag-staff, being found by the foregoing rules, to be $26^{\circ}30'$ seek $26^{\circ}30'$ in the Table of Horizontal Distances, which will be found 130; this number multiplied by 27, the height of the flag-staff gives 3510 feet, or 1170 yards, the distance between the ship and the battery.—Experience has taught the most able and best informed artillerist, that nothing in the practice of gunnery is more difficult than to judge *truly* of distances by eye, as it is called; and the more especially where objects are viewed across a deep ravin or valley: but with the Patent Telescope the distance of an object may be almost instantaneously found, if its height be known, even to a foot. The artillerist
may

may be perfectly master of his gun, know its point blank, and greatest range, according to its charge; but without knowing truly the *distance* of the object to be fired at; the gar-
 rison to be stormed; or fort to be silenced; much ammunition may be injudiciously and fruitlessly expended; and this did sometimes happen during the several campaigns upon the Continent, in the present contest:—one in-
 stance occurred where several most experienced gunners were found to be several hundred yards out in judging of a distance by eye; vary-
 ing, according to their respective judgments, from 100 to 300 yards, in a distance of some-
 thing less than a mile, or 1760 yards; in con-
 sequence of which much powder and ball were
 wasted without the least annoyance to the
 enemy.

There are situations where it is not practicable
 to measure the distance of an object from the
 ends of a base-line, by the rules of Trigonomet-
 ry. How valuable then must such an in-
 strument

strument be, as the one described, that will *always* give the distance by *one* observation if the extension of the object be known; as the height of a man, or the mean height of two, three, or four men, &c. &c. or by *two* observations, supposing the object inaccessible and unknown.

Suppose it be required to know the distance of an army, appearing in fight, on a plain; a fort, or garrison; or ship at sea; where it is next to impossible but objects enough of men, &c. will present themselves for ascertaining the distance at *one* station: but should it happen otherwise, the subtending angle of any, and the *same* object, at *two* stations, as will be presently shewn, will give the distance.

Viewing an enemy's camp on the opposite side of a river, its distance is required to see how far it is practicable to *annoy* it from certain situations; in this case, taking the
angles

angles subtended by any particular tent, that presents itself, in approaching the camp, at known distances from two observations, by a simple rule to be given, the true point blank distance may be easily found.—So that, by taking the subtending angle of a flag staff, &c. on a fortress; or the whole subtending angle of a ship at sea; or the angles subtended by its masts or yards, or ports, as circumstances may offer, the respective distances may be found; even supposing *all* the soldiers in the garrison or fortress, and *all* the seamen, to be out of sight; which, as before observed, is next to an impossibility to happen.—Hence the great use of the Patent Telescope, in a *military* point of view.

EXAMPLE 4.—Assuming the height of a man, merely for examples sake, (a soldier, for instance, under arms,) at 6 feet. Figure 4 in the Plate will shew the different angles he will subtend, at the several distant stations, of one, two,

two, three, and so on to six thousand feet, or two thousand yards. The intermediate, and farther distances, are found in the usual way; by entering the Table of Horizontal Distances, with the subtending angle of the known height of the man, or the mean height of two, three, or four men, which is found by dividing the sum of their angles by the number of men, *viz.* let the angles, subtended by three different men, be $6' 36''$; $6' 66''$; $6' 57''$; their sum amounts to $20' 39''$, which divided by 3, the number of men, will give $6' 53''$, the mean height; and this angle sought in the Table of Horizontal Distances, and worked as before taught, will give 3000 feet, corresponding to the angle, and distance of the third soldier, in Fig. 4, from the place of observation.—The converse of this, as in the first example, will prove true, and give the height of the soldier, the distance being known; for if 3000, the distance in feet, be divided by the nearest tabular number to $6' 53''$, the mean

F

angle

mean angle subtended, which will be 500, it will give 6 feet, the height assumed.

Again:—What will the height of a man be who is found to subtend an angle of $3' 54''$, at the known distance of a mile, or 5280 feet. Take out the number from the Table corresponding to $3' 54''$, which will be found to be 880; the distance 5280, divided by this number, gives, as before, 6 feet, the height of the man. Suppose the angle subtended to have been $3' 50''$, instead of $3' 54''$, at the same distance of 5280 feet, or 1 mile, the height of the man would, in this case, have been 5 feet $10\frac{1}{2}$ inches; for the divisor would have been 897, (*vide* Table) instead of 880.—In this way the distance is always found, from the known height; and, *vice versa*, the height from the distance.

To prove the last Example. The angle C. A. B. Fig. 2. whose arch line C. D. B. is equal

equal to radius A. B. brought into seconds, and multiplied by the given height of the man, 6 feet, and this product, divided by the subtended angle $3^{\circ} 54'$, rejecting fractions or thirds, will measure the distance 5280 feet, and all intermediate and greater distances may be proved by the same method;—rejecting remainders, beyond seconds of a degree, of the subtending angle, as of no consequence in *military practice*, as it will not amount to 6 inches in a hundred yards,—if greater nicety be required, as in Trigonometrical, &c. Surveys, the subtending angles of the object must be read off, and calculated to thirds, &c. of a degree; and the truth will then come out to mathematical precision.

The angles subtended by the soldiers, at every thousand feet, in Fig. 4. of the Plate, were those *actually proved* by the original Telescope, from which every other will be proved for public use, and the several distances were

ascertained to a foot. This *figure* also shews the exact proportion and comparative height of the men at the respective distances from the place of observation, and may be of great use to painters, as well as to military men.—In many fine landscapes, &c. where the figures of men and women have been introduced, either singly or in groupes, by painters of the first eminence, they have been most extravagantly in error in this respect, a due attention not having been paid to what is called *keeping*, or representing objects under their proper angles, or as they appear to the eye; and this want of *keeping*, or representing objects under very *different* angles from what they *really* do appear in nature, is very remarkable in one of the famous CARTONS OF RAPHAEL, representing the miraculous draught of fishes; and in the historical picture of Christ's transfiguration on the mount: the former makes the men appear of *full* size, and represents the boat so *small*, that, as observed by Mr. *Ferguson*, in his
Treatise

Treatise on Perspective, "any *one* of the men " seems sufficient to *sink* the boat." The latter makes CHRIST and his *disciples*, on the *top* of the mount, nearly as large as those at the *foot*, and the *mother* of the *boy* brought to be cured, though on her knees, nearly half the height of the mount; in which case, a spectator, at a little distance, could as well distinguish the *features* of those on the top of the mount as of those on the ground; a thing utterly impossible, had the *keeping*, or *true* angle that each subtended, been attended to.—View Fig. 4. again,—the angles subtended by the soldiers diminish in *true* mathematical proportion, and the features of the men appear less and less visible as they recede from the *eye* of the observer: this is *true* keeping.—Hence the Patent Telescope's usefulness to landscape and other painters, to find the *true* diminishing angle of all sorts of objects, presenting themselves to their view; particularly the more striking ones of distant hills, castles, churches, mills,

mills, groves of trees, &c. &c. as well as single figures, or groupes, of men, women, &c.

It would be useless to give more Examples to prove the truth and accuracy with which distances and extension of objects may be taken with the Patent Telescope; but having mentioned its usefulness to landscape painters, &c. to find the diminishing angles of distant hills, castles, churches, &c. it may be proper to say, that the diminishing angles of objects, and their distances, have been proved from a great variety of stations, and found to correspond very nearly to the truth of those mentioned in Major General Roy's Report of the Trigonometrical Survey. The places of observation, where other objects did not present themselves, for *trial* of the Patent Telescope, had *flag-staves* erected on them, where the distances did not exceed five or six miles. The places *observed from* were, Ditchling Beacon, Suffex; Chantonbury, Suffex; Leith-Hill, Surry; Riddlef-down,

down, Surry; Sevendroog-Castle, Kent; Hampstead;—Tower of Frant Church; Crouborough Beacon; Signal House at Beachy; Jevington Mill; and the place of Lewes Flag-Staff, in the county of Suffex.—The objects of known dimensions, to ascertain the respective distances were, the old Tower on Leith Hill; Horsham Church Spire; the Ball, &c. on St. Paul's Church, London; the Spire of Crouborough Chapel; Jevington Mill; Newberry's Tower, on Heathfield Down; Beachy Signal House; Seaford Signal House; Lewes Castle; Flag Staff on Mount Caburn; ditto on Mount Harry, near Lewes; ditto at Hollingbury Castle, near Brighton; &c. &c. Persons who have any knowledge of the above situations, or who will consult a Map, will allow that *variety* enough of stations have been taken; and *that* in almost every direction the distance of objects have been measured, and proved from fifty to six thousand feet, on the *original* base-line, near the Lewes Race Ground, and to the extent of upwards

wards of 22 miles, in the manner before described. Hence, again, the usefulness of the Patent Telescope, for *extensive* Trigonometrical Surveys; and, as will sometime hence be shewn, for all common surveys, superseding, in a great degree, the necessity of dragging a chain between stations to find the distances, and the content in acres; which will be done much quicker, and equally accurate, by this instrument, when fitted up as it is intended for that particular purpose.

Having sufficiently explained, and shewn how to find the *distance* of any object, from the place of the observer, when the *size* of the object is either known, or assumed, as illustrated by means of the 3 and 4 *Figures* on the Plate; and *vice versa*, where the *size* or *extension* of an object is to be measured, when its subtending *angle* is taken, and the *distance* known:—it remains to be shewn, and explained, in what way the *distance* and *size* of an object is to be found from

from the place or places of observation, when NEITHER of them is known.

PROB. II.

To find the *distance* and *size* of an object, when both are *unknown*.

Here, *two* subtending angles of the same object must be taken, at any convenient distances from each other, in a measured right line, approaching to, or receding from the object, as it may be most convenient, or at the places of any known radii, where the object can be seen.—The angles being taken as before taught.

To find the *distance*—the rule is, to multiply the larger angle into the *distance* between the *two* places of observation, and to divide the product by the difference between the *two* angles:—and, to find the *size* of the object, as

G

shewn

shewn in the 1st and 4th Example of Prob. I. divide the distance at either place of observation, by the Tabular Number, answering the nearest to the subtending angles.

EXAMPLE 1.—Let the *distance* and *size* of the object, D. B. E. (Fig. 5) from either place of observation, as at A. or C. be required. To find first the *distance*, and from thence the *size* of the object; apply the Telescope to the object, beginning at either station, suppose at A, and note the angle subtended; which let be 17'; pace, or measure, with a chain or staff, when great accuracy is required, any distance from A. to C, in a right line with the object, which suppose 45 feet; at C. apply the Telescope again, and suppose the angle to be subtended by the object, from this station, to be 20':—by the *rule*, multiply the larger angle, 20', into the measured distance between the places of observation at A. and C.—viz. 45 feet, and the product is 900 feet; this divided by

by the difference of the angles taken at A. and C. $17'$ and $20'$, which is $3'$, gives the distance of the object from the farthest station, at A, 300 feet; consequently, from the nearest station C. 255 feet. The distance of the object D. B. E. from both places of observation, being found, viz. from A. 300 feet to B. and from C. 255 feet to B, from these *data* to find the *height* or *size* of the object:---seek the Tabular number nearest to the angle subtended by the object at A. $17'$,—which will be found 202 ---the farthest distance 300 feet, divided by this Tabular number 202 gives 1.485; or if the distance be brought into inches, and divided as above, the answer will be 18 inches, nearly for the size or height of the object. Again: Seek the Tabular number nearest to the angle subtended by the object from the station at C. viz. $20'$, against which stand, 172; the less distance, from C. to the object, 255 feet, brought into inches, and divided by the above Tabular number 172, will also give 18 inches

G 2 nearly

nearly, for *size* or *height* of the object D. B. E. required.

The truth of the above rule is deduced from well known *data*.*

To prove this Trigonometrically at the farthest station A. the distance being 300 feet from the object : Say,

As rad.	90°.	—	10.00000
Is to <i>t</i> .	.17'.	—	7.69417
So is <i>y</i> . 300 feet, or 3600 inches			3.55630
To	<i>x</i> = 18 inches nearly		1.25047

Again,

* If *T*. denote the tangent of the larger, and *t*. that of the smaller angle, *d* the distance, between the *two* places of observation at A. and C; *y* the unknown distance of the object, from the farthest station at A; *y*—*d* the distance of the object from the nearest station, at C; *r* the radius, and *x* the unknown size of the object; then, in small angles, the tangents being as the angles; by the rules of Trigonometry, as $r : t :: y : x$ and $r : T :: y - d : x$; hence $rx = ty$, and $rx = Ty - Td$; therefore $ty = Ty - Td$, and $Ty - ty = Td$, which divided by $T - t$ gives $y = \frac{Td}{T - t}$: therefore the distance *y*, is equal to the product of the larger angle, multiplied into the distance between the *two* stations, and then divided by the difference of the two angles.

Again, at the nearest station C. the distance being 255 feet from the object : Say,

As rad. 90° . — 10,00000

Is to T. $20'$ — 7.76476

So is $y = d$. 255 feet, or 3060 inches 3.48572

To $x = 18$ inches as before. 1.25048

EXAMPLE 2.—Suppose the same object D. B. E. to be viewed under very different angles and distances, from the last example, its *size* or *height* must come out by the rule the same as before.—Let the *distance* be found as in the preceding Example. Applying the Telescope at station C. the angle subtended by the object is $5' 30''$ (i. e. the Index stands between the second and third division on the left hand, or Micrometer Scale; and the Vernier or Nonius appears to coincide with a little more than the 7-tenths, or 75 Centesms, which being doubled*, agreeable to former directions, gives $4' 15''$ Centesms—but

one

* This doubling the divisions, to find at all times the value of the angle on the scale, will not be repeated.

one hundred Centesims being equal to one minute, i. e. $6''$ to every 10 Centesims, 150 Centesims equal $1' 30''$ which added to the $4'$ the double of the two divisions, makes out the subtending angle of the object, as above, $5' 30''$). The measured or known distance between C. the nearest, and A. the farthest station or place of observation, let be 780 feet; let the angle of the object at A. be then taken, and found to be $3'$, then, by the foregoing rule, if the distance between the station A. and C. be multiplied into the larger angle of the object taken at C. $5' 30''$. or which will amount to the same thing using Decimal Figures, viz. 5.5 and the product be divided by the difference between $5' 30''$, and $3'$, which is $2' 30''$. or as before 2.5 using decimals instead of seconds; it will give the distance of the object from the farthest station at A. equal to 1719 feet, or as will be used for closer Logarithmic calculation, 20628 inches; and the distance between the stations A. and C. 780 feet or 9360 inches, being subtracted from
the

the quotient, or 20628 inches, leaves the distance of the object from the nearest station, 939 feet or 11268 inches. The logarithmic calculation will be *once* more shewn to prove the *size* or *height* of the object to be the same as before.

To find the *height* of the object D. B. E. from the farthest station A.

As rad.	90° —	10.00000
Is to <i>z</i> .	— .3'	6.94084
So is <i>y</i> .	20628 in.	4.31428
To <i>x</i> = 18 inches, as before		<u>1.25512</u>

To find and prove the *height* at the nearest station C.

As rad.	90° —	10.00000
Is to T.	— 5'. 30'	7.20408
So is <i>y</i> — <i>d</i> .	11268 in.	4.05150
To <i>x</i> = 18 inches, as before		<u>1.255548</u>

Example

Note, The distances are brought into inches for nicer logarithmic calculation.

EXAMPLE 3.—An army presenting itself on the opposite bank of a river, a soldier is observed standing close to the water's edge;—Required the breadth of the river?—Assuming the height of the soldier with hat and shoes at 6 feet, (but this is of no consequence, because the subtending angles at the two places of observation will always *prove* the height.) He appears to subtend an angle of $6' 25''$, which, by the rule of finding the distance, at a single observation, by taking out the tabular number for $6' 25''$, (in this case the mean of the two nearest numbers, *viz.* $6' 20''$ and $6' 30''$, or 543 and 529, added together, and divided by 2, will give a mean tabular number, 535, equal to the angle of $6' 25''$) which being multiplied as heretofore, by the height of the soldier, will give the distance 3210 feet, or 1070 yards, for the breadth of the river.—To prove both the soldier's height, and the distance or breadth of the river—let 900 feet, or 300 yards, be measured or paced back from the verge of the

the river, in a right line as suppose from C. to A. (Fig. 5,) and the subtending angle of the soldier be again taken, and found to be $5'$; if 900 feet, or 300 yards, the distance between the two stations, be added to the distance found by the first observation, it will make the distance of the soldier, from the farthest station, 1370 yards, or 4110 feet, which, divided by 6 feet, the soldier's assumed height, the quotient will be 685; the tabular number equal to $5'$, the angle subtended by the soldier at the farthest or last station.

The logarithmic proof to find the soldier's height will be, at farthest station, say,

As rad.	90° —	10.00000
Is to l .	— $5'$	7.16269
So is y .	4110 feet	3.61384
		<hr/>
To x . = 6 feet, as above		.77653
		<hr/>

H

At

At nearest station:
 As rad. 90° — 10.00000
 Is to Tan $6^{\circ} 25'$ — 7.27103
 So is y — d. 3210 feet — 3.50650
 To x. = 6 feet, as before — 77753

EXAMPLE 4.—Fig. 6. shews the western tower and part of the ruins of Lewes Castle, *before whose walls was fought the memorable battle between KING HENRY the THIRD and the BARONS on the 14th May, 1264.* There is nothing very materially different in this from the preceding Examples, only that, from the point C. to the Castle is a deep ravin or valley, and that the ground at C. is not favourable to form an accurate base-line to ascertain the distance from thence to the Castle by the rules of trigonometry, in the usual way, which is so readily done, as in the former directions, by the Patent Telescope. The distance, however, between the two places of observation, at A. and

and C. in this Example, is much greater than in any former one, which goes to *prove* that it is of no consequence, in point of distance, from whence the subtending angles of the objects are taken. Let it therefore be required to find the distance from the places of observation, A. and C. to the Castle; and from such *data* the size or height of the window D. B. E. Being too near the tower, at the first place of observation, C. to take into the field of the Micrometer the *whole* subtending angle of it, the window * presented itself as a favourable object to measure its distance; the angle subtended thereby was found to coincide with 7 micrometrical divisions, or 14'; but at station A. the same window subtended only 1 division and a half, or 50 centesims, equal to 3', the distance between the places of observation be-

H 2

ing

* Any object, as before observed, may be made choice of to find the distance, provided it can be well defined, at both places of observation, when *two* stations are used, viz. a window, pane of glass, chimney, course of stones, bricks, tiles, &c. &c.

ing 1200 yards, or 3600 feet, which, multiplied into the greater angle $14'$, gives a product of 50400; and this product, divided by the difference of the angles $11'$, the quotient will be 4581 feet 9-11, the greater distance from the place of observation at A.—the distance between the two stations at A. and C. subtracted from this number, leaves 982 feet, the distance from the place of observation at C. to the Castle window D. B. E. required. To find the *height* of the window, seek the tabular number coinciding with either angle $3'$ or $14'$, and let the greater or less distance be divided by it, and the height of the window will come out 4 feet, rejecting remainders, as of no consequence.

The

Greater distance.

Lesser distance.

$$\begin{array}{r} 4581 \\ \hline \end{array} = 4 \text{ feet.} \quad \begin{array}{r} 982 \\ \hline \end{array} = 4 \text{ feet.}$$

$$\angle 3' = 1146$$

$$\angle 14' = 245$$

The *distance* and *height* of LEWES CASTLE has been taken from all parts of the surrounding country, and at a great variety of distances, from 50 feet to 15 miles, merely to prove the truth and accuracy of the instrument; but, after the above number of Examples, it would be superfluous to add another, either to shew from whence the observations were made, or to illustrate the method of finding either distance or height, the direction for both being so simple the reader must, by this time, be well acquainted with it if the least attention has been paid to the foregoing rules.

ONE Nautical Example will be given, as quite sufficient for *that* practice.—To find the *distance*, and *size* or *height* of an object at SEA, is attended with a little more difficulty, owing to several causes; but the principal are, the irregular and almost constant *motion* of a SHIP, and the difficulty of measuring the *true* distance between *two* places of observation; but,

but, even here, if due care be taken, every thing may be ascertained with wonderful accuracy; it is however recommended to make use of *three*, instead of *two*, observations, to guard against any material error, where very great accuracy is required; and when the *distance* and *size*, or *height* of the object, are both required, and neither of them is known. As also in finding the distance of an island, cape, or head-land; either by taking *in* the angle subtended by the *whole* island, from its summit to the horizon, or by some prominent leading feature thereon, distinctly to be seen, and clearly defined, either approaching or receding from it.—It is also advisable to take the mean of *two*, or *three* observations, where the *distance* is required, from the *size* or *height* of a *known* object, which may be done in a few seconds if the ship is not violently agitated, and if she is sailing at the rate of *ten* or *twelve* knots an hour, the distance of her way, between the times of taking the observations,

can

can be but a few yards, which may be accounted for. The method of finding the mean angle is shewn in Ex. 4. Prob. 1. Page 321.

EXAMPLE 5.—Being at SEA, and observing an enemy's fort or battery, let it be required to ascertain its distance from the place of the ship, in three different situations, represented by A. B. C. Fig. 7. The flag-staff being distinctly visible from the farthest place of observation at A. is found to subtend an angle of $3'$, bearing right down upon the fort or battery in the direction A. B. and having run by the log 5348 yards, or a little more than a league to place B. another observation is taken, and the angle subtended by the flag-staff, at this place, is found to be $9'$.—From these *data* the distance from the fort or battery, as well as the height of the flag-staff, may be found by the foregoing rules, if the angles have been *truly* taken, and the distance between each place of observation as *truly* ascertained; to guard, however,

ever, against any error arising from the irregular motion of the ship, in not properly *defining* the object, or by not getting the *true* distant run by the log, between the places of observation A. and B.—the ship is kept in her course till she arrives at C. where another angle of the flag-staff is taken, of 40° the last distance run being given by the log 2072 yards: From these *data* then the several distances of the ship, at A. B. and C. from the battery or fort, may be *truly* found; and also the height of the flag-staff.—The height of the flag-staff, coming out the same from all the places of observation, A. B. and C. prove, to demonstration, the several *distances* run, the *angles* taken, and respective *distances* from the SHIP, at A. B. and C. to be all *true*.

To prove the distance and height of the flag-staff by the common numerical or simple rule:—The logarithmic, &c. having been sufficiently explained, need not be repeated.

To

To find first the *distance* of the SHIP, from the *fort or battery* at the several places of observation, and from *thence* the height of the *flag-staff*. — Let 5384 yards, the distance between the first and second place of observation, or between A. and B. be multiplied by 9', the angle subtended by the *flag-staff* at B. and this product be divided by 6', the difference between the two angles A. and B. the quotient will be 8022 yards, the *distance* of the *fort or battery* from the SHIP at A. the *first* place of observation; and if the *distance* between A. and B. 5384 yards, be subtracted from the whole distance, A. F. 8022 yards, the remainder 2674 yards, will be the *distance* from B. the place of the SHIP, where the *second* observation was taken, to the *fort or battery*, or rather to the *flag-staff* erected thereon: also, if the *distance* between the second and third places of observation, or between B. and C. or 2072 yards, be multiplied by 40', the angle subtended by the *flag-staff* at the *then* place of observation C. and

the product be divided by the difference of the *two* angles at B. and C. $40' - 9' = 31'$, the quotient will be as above 2674, the *distance* from B. to F. or from the *second* place of observation to the *fort or battery*: and the *distance* between B. and C. 2072 yards, or between the *second* and *third* places of observation, subtracted from the *distance* between B. and the *fort* 2674 yards, will give the *distance* 602 yards, from C. the *third* or *last* place of observation from the *flag-staff* on the *fort or battery*. The several distances then will be from A. to D. E. F. the *flag-staff* on the *fort or battery*, 8022 yards; from B. 2674 yards; and from C. 602 yards.

From the above *data* to find the *height* of the *flag-staff* D. E. F. and from *thence* to prove the foregoing observations of *angles* and *distances* to have been *truly* taken:—

Take

Take out from the Table of *Horizontal Distances* the tabular number for $3'$, the *first* subtended angle of the *flag-staff* from the place of the ship at A. 1146; if the *distance* between A. and the *fort*, 8022 yards, be divided by the above tabular number, the quotient will be 7, the *height* of the *flag-staff*, in parts of the same measure, the *distances* are found in, *viz.* yards.

Again:—The distance between station the *second*, or the place of observation at B. and the *fort*, 2674 yards, divided by the *tabular number* for the angle, at *this* station, $9'$, *viz.* 382, will give 7 for the quotient, the height of the *flag-staff* in yards, as before.

The *last* distance or place of observation, or from C. to the *fort*, 602 yards, divided by the *tabular number* for $40'$, *viz.* 86,—gives a like quotient of 7 yards, as in the *two* foregoing operations.

Thus do all the various *angles*, *distances*, and *heights*, prove each other, from *each* and *every* respective place of observation.

To bring the whole into *one* point of view in simple numbers—

The Tabular Numbers to the Angles are,

Angle.	Tab. Num.
A 3'	1146.
B 9'	382.
C 40'	86.

The several *distances* to the *Fort* or *Battery* from the places of observation, A. B. C. are as follow :—

$$\begin{array}{l}
 \text{Yds.} \\
 \text{A. B. or } 5348 \times 9' \quad \text{Yds.} \\
 \hline
 9-6 \quad = 8022, \text{ or distance from A. to F.} \\
 \text{B. C. or } 2072 \times 40' \\
 \hline
 40-9 \quad = 2674, \text{ or distance from B. to F.} \\
 \text{B. F. or } 2674 - \text{B. C. or } 2072 = 602, \text{ or dist. from C. to F.}
 \end{array}$$

Proof

Proof of the *Flag-staff's* height.

	Yds.	Yds.	Yds.
Dist.	A. F. 3022	B. F. 2674	C. F. 602
	$\frac{\quad}{\quad}=7;$	$\frac{\quad}{\quad}=7;$	$\frac{\quad}{\quad}=7.$ Yds
Tab. Num.	3' 1346	9' 382	40' 86
			Q. E. D.

Thus it appears clearly demonstrated above, that it is of no consequence what the *distance* is between station and station, so that the distances are *true* where more than *one* is taken, *i. e.* where *distance* and *extension* of the same object are required, both of them being *unknown*.

Hence, then, the value of the Patent Telescopic Micrometer, as a *nautical instrument*, for ascertaining distances and extension of objects at SEA, as well as on shore, and with *nearly* the same accuracy, if due care be taken, either by a *single* observation, from known *extension*, or by *two* or *three*, as circumstances occur, and when greater truth and accuracy are required, from unknown distance and extension.

To

To our *brave* TARS, who never want to know the *distance* or *size* of the ENEMY'S SHIP till they are near enough to board it, the Patent Telescope, in this respect, it will be allowed, can be but of *little use*; and, it is supposed, *this* was the reason why a *Noble* and *Gallant* ADMIRAL * would not even hear the *name* of the Patent Telescope, or any other instrument for measuring the *distance*, &c. of an ENEMY, mentioned than a TWO-AND-FORTY POUNDER; which, experience had taught HIM, gives, at one and the same moment, *their* DISTANCE and DURATION!!! But when the *Noble Lord* shall have been well assured of its usefulness in *other* respects, in *eclipses*, in *transits*, in *occultations*, in *lunar observations*, &c. he will doubtless form a more favourable opinion of it, as an instrument capable of answering many *valuable* NAUTICAL purposes, and indeed such as cannot well be dispensed with.

IT

* Duncan.

IT is true, that the *more* perpendicular the object, whose *distance* or *height* is required, is to the axis of the Telescope, the *more* exact will the result be; that an object upon any very considerable eminence, whose *distance* and *extension* is required, cannot be so *truly* taken by the foregoing rules, as if it were upon a *true* horizontal level; unless, as before observed, it be perpendicular to the axis of the Telescope: that a man placed at the top of St. Paul's, would subtend a much *less* angle from the iron railing at the bottom, than at *twice* the horizontal distance of its height:—or if the same man be placed on the summit of a high mountain, he will subtend a much less angle, (if perpendicular to the horizon, and oblique to the axis of the Telescope) than if viewed from the foot of the mountain, on the plain below, at *twice* the horizontal distance, where the mountain itself subtends a very considerable angle, at its base: but even here, the height of a man bears so inconsiderable a proportion to the altitude of a mountain, that, in *military* operations,

operations, it is of no consequence; neither is it in *nautical*, in measuring the distance between two ships, between a ship and an island, cape, harbour, fort, &c.—In trigonometrical, &c. surveys, it will be proper to make an allowance for the diminishing angle of objects, in proportion to their elevation, above the plain of the *horizon*, where objects are not viewed perpendicular to the axis of the Telescope, as before observed:—*And it is intended, some time hence, to adapt the Patent Telescopic-Micrometer to the purposes of surveying, when a suitable table of allowances for ALL elevations and depressions, to reduce hypotenusal to base lines, will accompany the instrument, fitted to a Theodolite.* The following table may, however, suffice for present *general* purposes, to shew what proportion, in distance, should be deducted to bring the hypotenusal to a base-line, from *four* degrees of elevation or depression, to *thirty-six*; beyond which it would be found useless to carry it either for *military* or *naval* purposes, it being near enough the truth, and sufficiently

extensive

extensive for both; to allow for the *range* of a gun, or to find the *distance* of an island, &c. &c.

Table of Allowances to reduce Hypothenufal to Horizontal Distances.

Deg.	Dist.	Deg.	Dist.
4°	$\frac{1}{400}$	20°	$\frac{1}{11}$
5	$\frac{1}{308}$	22	$\frac{1}{12}$
6	$\frac{1}{256}$	24	$\frac{1}{11}$
8	$\frac{1}{208}$	25	$\frac{1}{10}$
10	$\frac{1}{160}$	26	$\frac{1}{9}$
12	$\frac{1}{128}$	28	$\frac{1}{8}$
14	$\frac{1}{100}$	30	$\frac{1}{7}$
16	$\frac{1}{88}$	32	$\frac{1}{6}$
18	$\frac{1}{80}$	36	$\frac{1}{5}$

Suppose it be required to find the *horizontal distance* to a wind-mill, standing upon a hill, whose angle of elevation is known to be 12 degrees,—having found the hypothenufal or direct distance to the mill, by the foregoing rules, to be 1440 yards—against 12 deg. in the Table stands $\frac{1}{10}$ in the column marked Dist. which shews, that *one fortieth* of the hypothenufal distance is to be deducted to find the *true*

K

horizontal

horizontal distance; thus, $\frac{1}{16} = 36$ yards, is to be taken from 1440, which leaves the *true* horizontal distance 1404 yards.

Of Again:—Standing upon a hill, whose angle of depression to a house, in a meadow below, is 22° degrees, and whose hypotenusal distance is 2730 yards; required the *true* horizontal distance.—Against 22° deg. in the Table stands $\frac{1}{14}$, which shews, that *one fourteenth* of the distance is to be deducted from the hypotenusal or direct distance, to give the *true* horizontal distance— $\frac{1}{14} = 195$, which subtracted from 2730, the *hypotenusal* or *direct* distance, in yards, or other measure, leaves 2535, the *horizontal distance* required.

The following Table of Multipliers and Divisors for *all* general distances, from twelve inches to a league, will be found useful to expedite any calculation required in English measure.

Table

Table of Multipliers or Divisors for Finding Distances and Extensions.

Inches.	Feet.	Yard							
12	1								
36	3	1	Toise						
72	6	2	1	Rod					
198	16½	5½	1	chain					
792	66	22	11	4	1	Furl.			
7920	660	220	110	40	10	1	Mile		
63360	5280	1760	880	320	80	8	1	Leag.	
190086	15840	5280	2640	960	240	24	3	1	

Note. 60''' or Thirds, make 1" or Seconds.
 60" or Seconds, make 1' Prime or Minute.
 60' Primes or Minutes, 1° or Degrees.
 Equal to 69½ British Miles.

Having fully explained the *usefulness* and value of the *Micrometrical* part of the instrument as adapted to the *Telescope*, for *military*, for *naval*, and for all the general purposes of *Longemetry* and *Altimetry*, within its field or power; it remains to be shewn, in what way the in-

strument is useful and to be applied in *Microscopical Observations*.

As a Microscope it is capable of measuring the *lineal* and *comparative* dimensions of very small objects; and, in proportion to its magnifying power, is rather a thing of amusement than of any great use, except that it be to find the magnifying power of other Telescopes, which is done by measuring the diameter of the pencil of light at the eye of the Telescope, whose value is required; and when this pencil of light is well defined, it will shew the comparative value of the magnifying power of different Telescopes, as shewn by the Micrometer Divisions on the Scale.

The method of shewing the comparative value is this: Take the *first* and *second* tube, or that which goes by the name of the *eye-tube*, and the next to it, and apply the aperture of the second tube to the eye-end of the Telescope, whose comparative value is required, till

till by sliding the first tube backward and forward, as in bringing it to a focus for viewing objects, you clearly define the round pencil of light of the Telescope under examination, when the Scale of the Micrometer will point out its value. Thus may the comparative value of any number of Telescopes be found.

To use the instrument as a Microscope for examining small objects, and measuring their *lineal extension or dimensions*, let the *eye-tube* be unscrewed from the other parts; then by placing any small insect, or object of any kind, on a piece of white paper, and looking through the tube, moving it up or down, if held in a vertical position, or backward and forward, if horizontal, till the object be well defined*; the Micrometer Scale will then point out its lineal dimensions in hundredths or thousandths of an inch, by means of the Vernier or Nonius.

EXAMPLE

* Whether the instrument be used as a Telescope or Microscope, always slide the tube to the proper focus:

EXAMPLE 1.—Let it be required to find the diameter of hair.

Place the hair, as before directed, on a piece of white paper, and bring the central hairs or wires in one, as at *a*. Fig. 1. let the hair in question, whose diameter is required, be viewed through the eye-tube of the Telescope, brought to its proper focus; then by moving the nut or screw A. the central parallel hairs or wires will open and measure the diameter of the hair under examination, when the *Micrometer Scale* will shew its dimensions, to the thousandth part of an inch, if carefully observed.

EXAMPLE 2.—Placing a small insect under the tube, as before, suppose a small fly of any sort, whose *lineal* extension may be required, lay it at right angles to the hairs or wires of the Micrometer, thus +, then by turning the nut or screw A. as before, the central hairs or wires subtending the length of the fly, the *Scale*

Scale will give its measure, as in the former Example.

These Examples, and the method of examining small objects, are so very simple, that a repetition must be needless:—in this way may the whole body or limbs of an insect, or small object of any kind, be measured, where the *lineal extension* or comparative size is required.

IF the preceding pages have been read with the least tolerable degree of attention, it is impossible but the merest novice in the science of common numbers must be well acquainted with the method of performing all the examples illustrative of the *principles*, and various *uses* of the *Patent Telescope*,

It was never intended to go further into explanation than what would be just sufficient for practical use; and it is hoped enough has been
said,

said, and examples enough shewn, at large, to render every thing familiar and easy to perform.—Nothing further then seems necessary to be said than to advise and recommend to those who may *use* the *Patent Telescope*, either for finding the *distance* or *extension* of objects, or in any other respect to be *careful* in their observations.—To keep the instrument *firm* and *steady*.—To define the object under examination, very *nicely*, between the parallel hairs or wires.—To read off the subtended angle measured by the divisions of the *Micrometer truly*, together with the value of the *Vernier* or *Nonius*, (always **DOUBLING** the same for the *full* value of the angle.)—And to take out the tabular number, corresponding with the subtending angle, right. If then, the *last* part of the operation be *truly* performed by *multiplying* or *dividing* the tabular number, as before taught, the result will be, the *true* distance, extension, &c. of the object in any measure required.

FINIS.

ADDENDA.

AFTER the preceding pages had been printed, the following Problem; suggested by an officer of rank in the service, was sent to the Author, saying, "It may sometimes be of great consequence, in *military* operations, to be acquainted with the difference in elevation of particular objects," which the small, and very-general, table of allowances (p. 65) was never intended to give without calculating the perpendicular from well known *data*, (47th Eucl.) by extracting the square root of the difference of the base and hypotenuse.

It was mentioned in page 64, that the Patent Telescope would sometime hence be adapted to the business of *surveying*, when a suitable table would accompany such instrument, which would fully answer the purpose of solving *all* the properties of a triangle, right or oblique, being, in its present form, calculated to ascertain *point blank* distances, and the size or extension of objects only, and not their difference of level or bearings from each other. The bearings and angles of elevation or depression, if required, must therefore be found by a quadrant, or other instrument; then will the additional *new* epitomized table, (p. vi,) by simple multiplication or division, solve the problem, fig. 1. pl. 2. proposed, and all similar ones; and will be a *datum* for the more readily solving those of an oblique kind also.

PROBLEM

PROBLEM PROPOSED.

“ To reduce hypotenusal to horizontal distances, and to ascertain the difference in height of two places.

“ Let A and C, (fig. 1. pl. 2.) be the two places, A, being the place of observation; A, C, the hypotenusal distance (suppose 150 yards) taken by the telescopic micrometer; d, e , the depression, taken by a theodolite (or quadrant) suppose 16° .

To solve the above.

“ Search in the nautical tables, traverse table, Hamilton Moore's Epitome, tab. III. (or any other,) for the table shewing the difference of latitude and departure for 16° , that is to say, the table shewing the value of all the sides of the rectangular-triangle, of which *one* acute angle A,

and *one* side, A, C, are known; and then 150, hypothenuſal diſtance, gives for A, B, $144\frac{1}{10}$ horizontal diſtance; and $41\frac{1}{10}$ for B, C, difference of height."

It having been obſerved, that the table, p. 65, calculated on very general principles to find the horizontal diſtance of objects *only*, and not their *perpendicular* height, could *not* ſolve the above problem; as far, however, as it is adapted, it will give *nearly* the ſame reſult as the above, or any other nautical tables; for, if the allowance, in table, p. 65, oppoſite to $16^{\circ}=\frac{1}{10}$, be deducted, as before taught, it will give 144 yards for the horizontal diſtance A, B, of the problem, differing only two tenths of a yard from the nautical tables:—but this will not *always* come out ſo near the truth. The following table, however, calculated on the nautical principles, and epitomiſed, to get rid of a cumbersome maſs of figures, which may be diſpenſed with in military practice, will give the ſame, or

nearly

nearly the same, result, at all elevations and de-
 pressions, and be a *datum* for finding the distance
 B, C, fig. 3. pl. 2. or any similar distance.

To illustrate this by a few examples :

EXAMPLE I.

Let the *above* problem be taken where the
 hypotenuse, or distance A, C, fig. 1. p. 2. equals
 150 yards, and the angle of depression, *d, e*,
 equals 16° , are given to find the base, or hori-
 zontal side, A, B, and the perpendicular B, C.

Rule to find the horizontal distance A, B:—
 Multiply the hypotenuse by the tabular num-
 ber, in the second column, opposite the given
 angle, marked at the head of the table Hor.

Thus, if the hypotenuse, or distance, A, C, .
 = 150, be multiplied by .961, the tabular num-
 ber for 16° , it will give 144. and leave a deci-
 mal

FOR MILITARY, &c. PRACTICE.

NEW TABLE

FOR COMPUTING THE HORIZONTAL SIDE OR BASE, AND
PERPENDICULAR OF A RECTANGULAR TRIANGLE;
WHEN THE HYPOTHENUSE AND ONE ACUTE ANGLE BEING KNOWN.

Dec	Hor.	Per.	Dec	Hor.	Per.	Dec	Hor.	Per.	Dec	Hor.	Per.
1	1.	57.2	23.	92	2.36	45.	707	1.	67.	391	424
2	.999	28.8	24.	913	2.24	46.	694	.966	68.	374	404
3	.998	12.9	25.	906	2.14	47.	682	.933	69.	358	383
4	.997	14.24	26.	898	2.05	48.	669	.9	70.	342	364
5	.996	11.4	27.	891	1.96	49.	656	.869	71.	325	339
6	.994	9.5	28.	882	1.88	50.	642	.839	72.	309	325
7	.992	8.13	29.	875	1.80	51.	629	.809	73.	292	305
8	.990	7.1	30.	866	1.73	52.	615	.781	74.	276	287
9	.988	6.3	31.	857	1.66	53.	602	.758	75.	259	268
10	.984	5.65	32.	848	1.6	54.	588	.726	76.	242	249
11	.982	5.15	33.	839	1.54	55.	573	.7	77.	225	231
12	.978	4.7	34.	829	1.48	56.	559	.674	78.	208	212
13	.974	4.35	35.	819	1.42	57.	544	.649	79.	191	194
14	.970	4.	36.	808	1.37	58.	530	.625	80.	174	1766
15	.966	3.73	37.	799	1.32	59.	515	.601	81.	156	1579
16	.961	3.49	38.	788	1.28	60.	.5	.577	82.	139	1404
17	.956	3.27	39.	777	1.235	61.	485	.554	83.	122	1228
18	.951	3.08	40.	766	1.19	62.	469	.531	84.	104	1052
19	.945	2.9	41.	755	1.15	63.	454	.509	85.	87	0874
20	.940	2.74	42.	743	1.11	64.	438	.487	86.	69	0698
21	.933	2.6	43.	731	1.071	65.	423	.467	87.	52	0520
22	.927	2.47	44.	719	1.034	66.	407	.445	88.	35	0350
									89.	018	0180

mal remainder of .15 instead of .2, approximating near enough the truth for any *military* operation.—For *nautical* purposes, the nautical tables are always at hand on board ship, and may be used, if preferred.

8 Rule to find the perpendicular B, C :—Divide the horizontal distance, above found, by the tabular number, in the third column, marked Per. opposite the given angle, and the quotient will come out 41.3, the perpendicular B, C, required, in any measure of the hypotenuse given.

EXAMPLE II.

Required the distance between two forts, or two ships, B, C, fig. 2, pl. 2. their distance from A, the place of observation, being equal, suppose 1250 yards; and the bearing from each other 34° .—Here, the angle being isosceles, form it into two right angled triangles, A, D, B, and A, D, C;— b, c , and c, d , will then be equal to 17° .

Multiply

Multiply the tabular number opposite 17° .956 into the distance A, B; cutting off the decimal figures, leaves 1195, the horizontal distance A, D; this, divided by its proper tabular number 3.27, gives 365.4 for B, D, or C, D, which, being added together, gives the distance from fort to fort, or from ship to ship, 730.8 yards required.

EXAMPLE III.

In the scalenous, or oblique-angled triangle, A, B, C, fig. 3, pl. 2, the distance A, B, 1050, and A, C, 1432 being found, by the telescope, as before, required the distance from B to C.

It will naturally suggest itself that this is one of the most useful problems in this branch of military or naval tactics; and, although the epitomised table will not give the distance B, C, so readily as the perpendicular B, D, is found, it will furnish *data* to solve the problem as truly;

truly; and, probably, as soon, as the nautical
tables, to persons unaccustomed to search in
such tables.

30 Taking A, B, 1050 yards, as hypothenuse to the assumed base, A, D, in the line, A, C, and multiply, as before, the tabular number corresponding to the subtended angle, $f, g, 12^\circ$, which will be found in its proper column, .978, the produce, 1027, will equal A, D, which divided by the tabular number in the next column for perpendicular, 4.7 will give B, D, equal 218.—Taking A, D, from A, C, leaves 405 equal, D, C; having then B, D, = 218 and D, C, = 405, the distance from B to C, 460, is found by extracting the square root from the sum of the squares of B, D, and D, C; or in any nautical traverse table

In the mechanical construction of any instrument, mathematically true in principal, much depends upon the nature of the materials with which

which it is formed, and much on the skill and ingenuity of the artist. It is, therefore, next to an impossibility that every instrument, even from the hands of the same artist, should be found *exactly* alike, though all will give the same result, when practically applied, if due attention be paid to the foregoing, and following directions; which it was thought proper to mention, in the Addenda, where *great* accuracy is required in ascertaining distances.

It was mentioned, page 15, that the *whole* divisions, on the scale of the micrometer, were minutes of a great circle; this, as above observed, is mathematically true; but the difference between a mathematical and a physical line, necessarily renders the divisions of the micrometer scale liable to a small error, proportioned to the manner in which they are executed;—the different refracting powers of the lenses, and the strength of the lines, forming the divisions of the micrometer scale, will also cause a variation

of

of a few seconds in the value of *some* of the telescopes:—The mean value, therefore, of each single division, will be engraved on the tube of every one, to be properly allowed for.

Where great accuracy is required in ascertaining a distance, the size, or extension, of an object, or the difference in point of elevation of *two* objects, a single second is of some consequence, and it will be proper to add to the division, or divisions, which any object is found to subtend, the mean value of the seconds (and even *thirds* in astronomical observations) due to each division, the loss in value, occasioned by the difference before mentioned, between a mathematical and a physical line. Suppose the mean of each division should be found equal to $1' 2''$, or other number of seconds, and that an object subtends 3 divisions, which, *doubled* as directed, gives $6'$; instead, therefore, of entering the table of horizontal distances with $6'$, to find the distance, the $2''$ must be added to every *single* division,

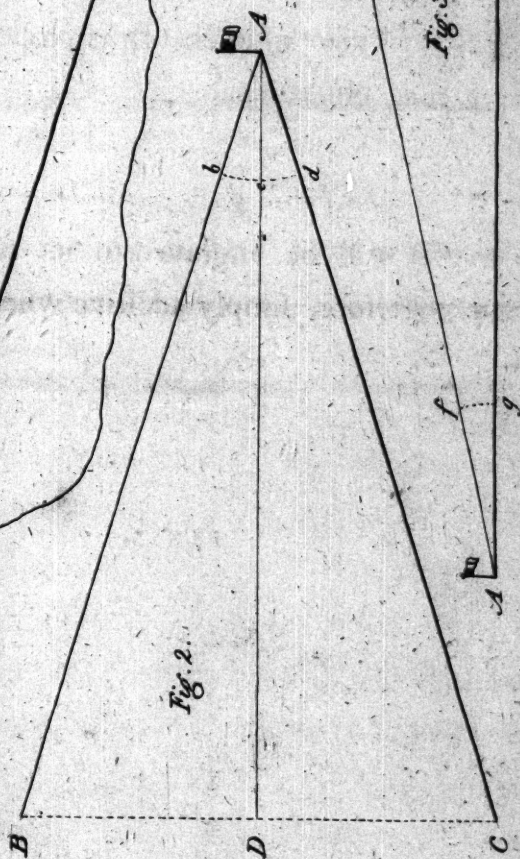
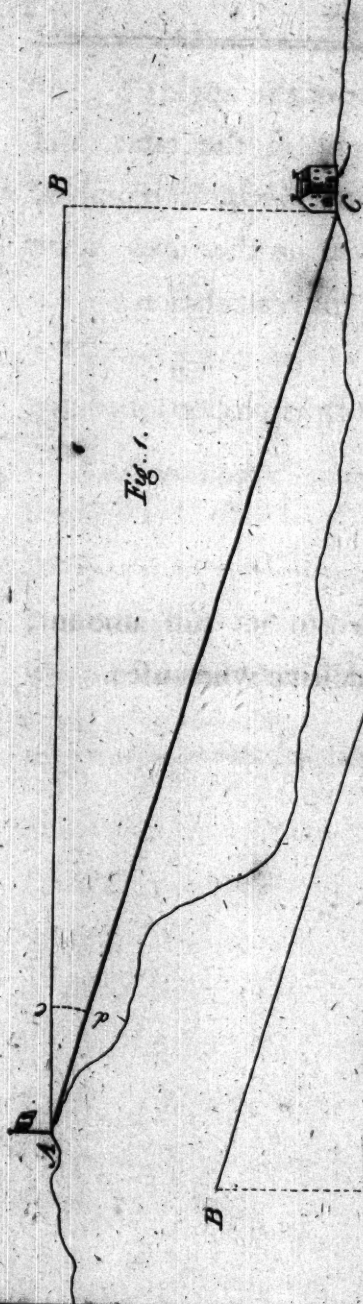
b 2

fion, to make up the value of the angle; $6' . 12''$ must, therefore, be sought in the table, and in *this* way the seconds and thirds, if required, wherever they are engraved on the tubes of the telescopes, must be taken into calculation.

The vernier must be thus proportioned for very nice observations.

The fixed value will require no such correction; it will be engraved to its full amount, and, therefore, simply additive when used.

FINIS.





ERRATA.

- Page 17, fifth line from the bottom, for *issofeles*, read *isofeles*
— 65, third line of table, for $\frac{1}{110}$ read $\frac{1}{150}$
— 67, third line from the bottom, for *longemetry* read *longimetry*
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